

# Analysis of the system of pricing of railway capacity allocation in the Czech Republic

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**Abstract.** The introducing of legal background for capacity allocation in Czech Republic. The analysis of price for capacity allocation in Czech Republic and in Europe. The proposal of the capacity allocation price which should lead the Railway undertaking's path request to the suitable product. Possible impact of the price of capacity allocation to Railway undertaking's decision about the railway transport.

## Introduction

Railway capacity is allocated using two basic modes, i.e. within processing the annual timetable and its changes, and in an ad hoc request mode. As for timetable 2017, the following (4) products are offered to applicants for railway capacity:

- 1) Regular request for railway capacity allocation to be taken into account when creating the annual timetable – "RJ",
- 2) Late request for railway capacity allocation to be taken into account when creating the annual timetable – "PJ",
- 3) Request for railway capacity allocation until the next change of the annual timetable – "ZJ",
- 4) Individual ad hoc request for railway capacity allocation.

As for individual ad hoc requests for railway capacity allocation, the applicants can use the following products:

- a) Ad hoc request for railway capacity allocation submitted 3 and more working days before the first requested date of train departure (including the request date) – "N3",
- b) Ad hoc request for railway capacity allocation submitted later than 3 working days before the first requested date of train departure (including the request date) – "P3" (residual railway capacity),
- c) Ad hoc request for railway capacity allocation for technical and safety tests – "TB",
- d) Ad hoc request for railway capacity allocation for test rides of vehicles of unapproved type or rides at a speed exceeding the track speed – "ZK",
- e) Ad hoc request for railway capacity allocation for Railway Infrastructure Administration infrastructure maintenance – "UI",
- f) Ad hoc request for railway capacity allocation due to Railway Infrastructure Administration infrastructure restrictions – "OM",
- g) Ad hoc request for railway capacity allocation for other reasons attributable to the Railway Infrastructure Administration – "JD".

## 1. Railway Infrastructure Administration products related to capacity allocation

Train route and train timetable are determined in assessing the request for railway capacity allocation. For requests for products RJ, PJ, ZJ, N3, TB and ZK, the timetable is created with conflict resolution.

As for requests for products P3, UI, OM and JD, it is up to the allocator to decide whether to allocate ad hoc routes with conflict resolution, or routes within the residual railway capacity without resolving the conflicts. For routes within the residual railway capacity, conflicts are later resolved by operational employees of the

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infrastructure manager. Table 1 clearly shows that railway undertakings are increasingly using ad hoc requests compared to requests to be taken into account when creating the annual timetable.

This has been a trend for railway undertakings EU-wide due to the increasing demand for greater flexibility, mainly in freight transport. The authors thus tried to summarise the advantages and disadvantages of both railway capacity allocation modes for railway undertakings.

Table 1. Evolution of the number of data timetables for the train traffic diagram 2005–2016

Year	Number of routes requested for the annual timetable	Number of ad hoc allocation requests
2005	15,468	62,970
2006	14,836	78,595
2007	15,213	127,547
2008	14,366	159,021
2009	14,403	161,223
2010	13,381	180,602
2011	13,107	185,100
2012	12,706	181,647
2013	12,023	205,993
2014	11,704	240,460
2015	13,361	252,797
2016	14,959	266,610

Source: Authors according to (16)

#### **Mode of allocation within the annual timetable – products RJ, PJ and ZJ**

Each of the railway capacity allocation modes has its advantages and disadvantages.

Advantages of requests for railway capacity allocation to be taken into account when creating the annual timetable:

- higher quality of timetable processing,
- priority processing,
- determination of technologies at originating, intermediary, destination and frontier stations,
- with a higher number of route-days, the price of railway capacity per route-day is lower.

Disadvantages of requests for railway capacity allocation to be taken into account when creating the annual timetable:

- greater risk of sanctions for unused railway capacity due to a large time gap between the time of booking the route and the actual train ride,
- low flexibility of changes for railway undertakings,
- greater limitation by the booked route parameters (where the business case changes, the railway undertaking has to submit an individual ad hoc request for railway capacity allocation – e.g. upon extension of the original route).

#### **Ad hoc allocation mode – products N3, P3, TB, ZK, UI, OM and JD**

Individual ad hoc requests for railway capacity allocation have their advantages and disadvantages as well.

Advantages of individual ad hoc requests for railway capacity allocation:

- greater flexibility for railway undertakings,
- greater probability of using the route, and thus a lower risk of sanctions for unused railway capacity,
- lower price of railway capacity allocation with a lower number of route-days, more flexible adaptation to changing market requirements.

Disadvantages of individual ad hoc requests for railway capacity allocation:

- lower quality of timetable processing (mainly in residual railway capacity routes) without conflict resolution,
- lower priority in timetable processing,
- need for the railway undertaking to negotiate technologies at stations (originating, intermediary, destination and frontier) on a case-by-case basis,
- impossibility to use certain tender prices, e.g. tender price J.

With the increasing number of requests for railway capacity allocation, mainly in the ad hoc mode, it is necessary to manage the railway undertakings to submit their requests for railway capacity allocation in time to ensure a timely and high quality processing of timetables, and to prevent them from submitting requests in the annual timetable allocation mode, which are ad hoc requests in nature. One of the ways to motivate the railway undertakings to use appropriate products is pricing the products in a way that the railway undertakings get the best value for money, and the price covers the costs reasonably incurred in railway capacity allocation at the same time.

Railway Infrastructure Administration products related to capacity allocation and their prices (for timetable 2017) are shown in Table 2. Coefficients K1, K2, and K3 are rates used in formula (1) to calculate the price of railway capacity allocation.

Table 2. Railway Infrastructure Administration products related to capacity allocation for timetable 2017

<b>Product</b>	<b>K1</b>	<b>K2</b>	<b>K3</b>
<b>RJ</b> regular request for railway capacity allocation to be taken into account when creating the annual timetable	1,700	8	10
<b>PJ</b> late request for railway capacity allocation to be taken into account when creating the annual timetable	1,700	10	20
<b>ZJ</b> request for railway capacity allocation until the regular change of the annual timetable	1,700	10	20
<b>N3</b> ad hoc request for railway capacity allocation submitted 3 and more working days in advance	100	0	70
<b>P3</b> ad hoc request for railway capacity allocation submitted later than 3 working days in advance	100	0	160
<b>TB</b> ad hoc request for railway capacity allocation for technical and safety tests of railway vehicles	480	0	70
<b>ZK</b> ad hoc request for railway capacity allocation for test rides of vehicles of unapproved type or rides at a speed exceeding the track speed	960	0	70

Source: (4)

The payment for railway capacity allocation was introduced in 2004 (before 2004, railway capacity allocation was not subject to a charge) to regulate the behaviour of railway undertakings in railway transport planning.

The system was devised as a rate times the number of route-days (days the train spends on the route). Originally, 3 rates had been determined as follows: CZK 15 per route-day for allocation within the annual timetable, CZK 25 per route-day for requests submitted 3 and more working days before the first day of the train ride, and CZK 120 per route-day for requests submitted later than 3 working days before the first day of the train ride (residual railway capacity). These rates had applied until 2010.

With timetable 2013, rates K1, K2 and K3 were introduced, and in addition to the rate per route and route-day, rates per kilometre of the planned route started to be charged as well. K1 is the price of processing and determining of the timetable and railway capacity allocation, K2 is the price of train route creation, and K3 is the price of train route allocation per day.

K1 amounting to CZK 1,700 applies to all products within the annual timetable (regular request, late request and request until the next change of the annual timetable – products RJ, PJ and ZJ), and K2 in the amount of CZK 100 applies to ad hoc requests for railway capacity submitted 3 and more working days in advance (product N3) and requests for railway capacity submitted later than 3 working days in advance (product P3). K1 for ad hoc requests for railway capacity allocation for technical and safety tests of railway vehicles remained at CZK 480 (product TB), and for ad hoc requests for railway capacity allocation for test rides of vehicles of unapproved type or rides at a speed exceeding the track speed remained the same as well (CZK 960) (product ZK).

K2 for RJ was fixed at CZK 8 per 1 route kilometre, and for products PJ and ZJ at CZK 10 per 1 route kilometre. For the other products N3, P3, TB and ZK, K2 was fixed at CZK 0 per 1 route kilometre.

K3 for RJ is CZK 10 per day of train route allocation, for PJ and ZJ it's CZK 20 per day of train route allocation, for N3 it's CZK 70 per day of train route allocation. For P3, K3 was fixed at CZK 160 per day of train route allocation and for TB and ZK, K3 amounts to CZK 70 per day of train route allocation.

Revenue from railway capacity allocation should cover the total direct costs of railway capacity allocation, but cannot exceed them. Using MS Excel, prices of railway capacity allocation will be modelled that would take into account all economically justifiable costs of railway capacity allocation, and would motivate railway undertakings to book the individual products in an optimal way at the same time.

## **2. Requests for railway capacity allocation**

To properly regulate the demand of railway undertakings for individual products, it is first necessary to define the requirements on target groups of these respective products.

### **2.1 Requests for railway capacity allocation to be taken into account when creating the annual timetable and its changes – products RJ, PJ and ZJ**

These products are meant for requests for high-frequency train rides (ideally with daily frequency) requiring the creation of a fixed train route to be strictly adhered to and containing other requirements:

- creation of transfer connections,
- creation of passenger service train cycles,
- creation of offered departure or arrival times,
- determination of technologies at originating, intermediary, destination and frontier stations.

The requests are submitted at the times agreed on European level, and timetables proposed by capacity allocator are submitted at the times defined by national legislation and European agreements as well.

#### **a) Regular request for railway capacity allocation to be taken into account when creating the annual timetable – product RJ**

For RJ, requests are processed with highest quality (in a "blank" train traffic diagram sheet). Subsequently, detailed information is provided on the timetable implementation in a train diagram, working timetable and booking timetable. A RJ request should be more cost effective than PJ or ZJ ones for the applicants to be motivated to submit requests earlier, which is advantageous for creating a timetable as there is more time for the route creation. With a higher number of route-days, the price of railway capacity per route-day should be lower. The proposed price of RJ, PJ and ZJ should also be lower for railway undertakings than the price of N3 for a number of route-days greater than the limit number.

#### **b) Late request for railway capacity allocation to be taken into account when creating the annual timetable – product PJ**

PJ is meant for requests submitted after the regular request deadline. For these requests, it is not always possible to guarantee the requested time frame, the route is created within an already created timetable, and the necessary effort is similar, or slightly higher than for regular requests.

The proposed price should be higher than for RJ requests.

#### **c) Request for railway capacity allocation until the next change of the annual timetable – product ZJ**

ZJ is meant for requests which compared to ad hoc requests require higher quality and the processing of the necessary instruments is more demanding. The route creation (within an already created timetable) is similar and requires similar effort as in late requests. The proposed price should be higher or the same as in late requests.

### **2.2 Individual ad hoc requests for railway capacity allocation – products N3, P3, TB, ZK, UI, OM and JD**

This category includes individual and less frequent requests within the period between timetable changes, and sometimes also longer-term requests with a departure date within the period between timetable changes (with limited requirements on links to other requests or on defining arrival and departure time frames for selected stations).

#### **a) Individual ad hoc request for railway capacity allocation submitted 3 and more working days in advance – product N3**

For this request, a timetable is created within a period between timetable changes, which is then included in the next timetable change. These are often requests in response to planned closures, and the route creation requires similar effort as in requests until the next change of the annual timetable. What is different is the lower quality of timetable information, requiring railway undertakings to use more information sources.

In some cases, there is a need for more consultations with railway undertakings, technologists, etc., and the processing effort is thus higher. For a number of route-days greater than the limit number, the proposed price of N3 should be higher than for ZJ, but at the same time lower than for P3.

#### **b) Individual ad hoc request for railway capacity allocation submitted later than 3 working days in advance – product P3**

P3 includes one-time, casual or irregular transport requests (the applicant doesn't know the exact ride date in advance) submitted very shortly before the actual ride. There is less time for request processing and time frame allocation (in extreme cases only in the order of minutes), and conflicts between the new route and existing ones are not resolved at the route creation stage (they are only resolved operationally later). The requested and actually allocated route parameters differ more than in above mentioned requests, timetable quality is lower, the most important criteria being the speed of processing whilst respecting a certain level of route safety (sticking to absolute route parameters), and giving all necessary information on the route to all operational employees. Technologies at originating, intermediary, destination and frontier stations are negotiated by the railway undertaking on a case-by-case basis. The proposed price should be higher than for N3 requests.

**c) Individual ad hoc request for railway capacity allocation for technical and safety tests of railway vehicles, for test rides of vehicles of unapproved type or rides at a speed exceeding the track speed – products TB and ZK**

Categories TB and ZK include requests for railway capacity allocation for technical and safety tests of railway vehicles, for test rides of vehicles of unapproved type or rides at a speed exceeding the track speed, submitted by railway undertakings in the individual ad hoc mode as these types of train rides are not made regularly, but only as needed, and the exact date of these rides cannot be predicted long time in advance.

The proposed price of railway capacity allocation (for TB and ZK) must reflect the highly demanding nature of request processing, as finding a suitable route and creating a timetable with the necessary measures is time consuming due to a greater need to consult several aspects of route allocation, and the costs of the necessary instruments are higher due to several technical and organisational measures required for the train ride. The request must be submitted for processing more than 3 working days before the intended departure date. The proposed price is based on the price of N3, taking into account route creation specifications.

**d) Individual ad hoc request for railway capacity allocation for maintenance, restoration and increasing of usable capacity – products UI, OM and JD**

For train rides made in connection with diagnostics and maintenance of infrastructure of the Railway Infrastructure Administration (UI, OM and JD), i.e. for the needs of the Railway Infrastructure Administration, 100% discount is provided on railway capacity allocation. For train rides made due to infrastructure restrictions attributable to the Railway Infrastructure Administration (i.e. planned and unexpected closures and irregularities), capacity is provided for free, these being rides capacity has already been allocated for (train redirections), or railway undertakings' rides due to infrastructure restrictions which otherwise wouldn't be necessary (bringing and carrying away necessary items).

The aim of the regulatory function of the price of railway capacity is to regulate requests so that long-term requests are submitted in the mode of the annual timetable and its changes, and short-term requests in the ad hoc mode. At the same time, it is necessary to take into account the effort and processing quality, and the following:

- a) Quality of route creation and the effort required,
  - dependence on route length and the necessary negotiations with other entities,
  - passenger trains – negotiation with state administration – with ordering railway undertakings,
  - adopting other measures related to the route use,
  - dependence on the length of the period of route use, as the probability of finding a suitable route decreases and its creation becomes more complicated, and the probability of free slots being occupied by requests submitted earlier increases,
- b) Quality of the necessary instruments and the effort required,
  - creation of a train diagram and working timetable,
  - creation of a booking timetable for passengers,
  - creation of a data timetable and its distribution to subsequent information systems,
- c) Time period of train route use – route booking.

The maximum number of route-days for regular and late requests and requests until the next change of the annual timetable established by the authors is based on the deadlines for the creation of the annual timetable and its planned changes, the maximum number of route-days for individual ad hoc requests submitted 3 and more working days in advance is based on the defined requirements on target groups of requests for individual and less frequent requests within the period between timetable changes, and sometimes also longer-term requests with a departure date within the period between timetable changes. The maximum number of route-days for individual ad hoc requests submitted later than 3 working days in advance starts from the assumption of the most inconvenient accumulation of Christmas bank holidays (3 working days, 3 bank holidays on working days and twice 2 weekend days).

Table 3. Allocated data timetables in 2016 by products in the annual timetable

<b>Allocated data timetables in 2016 – by products in the annual timetable</b>				
	<b>RJ</b>	<b>PJ</b>	<b>ZJ</b>	<b>Total</b>
Number of data timetables	13,686	788	485	14,959
Number of route-days	2,899,051	132,265	32,170	3,063,486
Total length [km]	731,593	37,661	33,727	802,981
Total price [CZK]	58,109,454	4,361,513	1,805,166	64,276,133
Average number of route-days per data timetable	211.8	167.8	66.3	204.8
Average length [km per data timetable]	53.5	47.8	69.5	53.7
Average price [CZK per data timetable]	4,245.9	5,534.9	3,722.0	4,296.8

Source: Authors according to (23)

The difference between the allocated data timetables and allocated route-days, as shown in Table 3, consists in the fact that one data timetable can be allocated for more route-days. The Table shows the calculated average number of allocated route-days, route length and price of railway capacity allocation by products in the year concerned in the annual timetable mode.

Table 4 shows the difference between allocated data timetables and allocated route-days in the ad hoc mode. The Table also shows the calculated average number of allocated route-days, route length and price of railway capacity allocation by products in the year concerned in the ad hoc mode.

Table 4. Allocated data timetables in 2016 by ad hoc products

<b>Allocated data timetables in 2016 – by products in the annual timetable</b>					
	<b>N3</b>	<b>P3</b>	<b>TB</b>	<b>ZK</b>	<b>Total</b>
Number of data timetables	13,534	159,968	196	285	173,983
Number of route-days	26,400	160,943	196	367	187,906
Total length [km]	1,357,650	11,491,204	9,742	11,492	12,870,088
Total price [CZK]	3,201,400	41,747,680	107,800	299,290	45,356,170
Average number of route-days per data timetable	2.0	1.0	1.0	1.3	1.1
Average length [km per data timetable]	100.3	71.8	49.7	40.3	74.0
Average price [CZK per data timetable]	236.5	261.0	550.0	1,050.1	260.7

Source: Authors according to (24)

Table 4 does not contain products UI, OM and JD (ad hoc products); even though these represent a considerable number of allocated data timetables, route-days and kilometres of route length, they do not factor in the price of railway capacity allocation as their price hasn't been set.

The price of railway capacity allocation is calculated using formula (1):

$$CK = K1 + K2 \cdot Dtr + K3 \cdot Pdj \text{ [CZK]} \quad (1)$$

Where:

*CK* is the total price of railway capacity allocation [CZK],

*K1* is the price of processing and determining of the timetable and railway capacity allocation [CZK],

*K2* is the price of train route creation [CZK per km],

*K3* is the price of train route allocation per day [CZK per day],

*Dtr* is the route length; the distance between point of origin and point of destination on railway network, where the Railway Infrastructure Administration functions as infrastructure manager, or capacity allocator [km],

*Pdj* is the number of route-days the route is allocated for [day].

Based on formula (1), the authors calculated limit values for the number of allocated route-days of the individual products subject to charge in the annual timetable, i.e. RJ, PJ, and ZJ. For requests matching the product definition, a condition was set stipulating that products in the annual timetable mode must be more cost effective than ad hoc products for a number of days greater than the limit number. A one-time ride in the annual timetable mode will always be more expensive than in the ad hoc mode. As a result, the following limiting conditions:  $RJ < N3$ ,  $PJ < N3$ ,  $ZJ < N3$  and motivational conditions:  $RJ < PJ$  and  $N3 < P3$  can be formulated. Limiting conditions apply to a number of days greater than the limit number and motivational conditions apply to an arbitrary number of route-days. The current limit values were calculated using average values (Table 5) of individual products from the 2016 dataset.

Table 5. Allocated data timetables in 2016 by ad hoc products

<b>Allocated data timetables in 2016 – by products in the annual timetable</b>					
	<b>RJ</b>	<b>PJ</b>	<b>ZJ</b>	<b>N3</b>	<b>P3</b>
Average number of route-days per data timetable	211.8	167.8	66.3	2.0	1.0
Average route length [km per data timetable]	53.5	47.8	69.5	100.3	71.8

Source: Authors

The authors modified formula (1) to fit inequations to calculate limit values for allocated route-days for products RJ, PJ and ZJ (annual timetable) compared to product N3 (ad hoc).

The limit values were calculated to establish the break-even point in the number of route-days, based on which requests should be moved from the ad hoc mode to the respective products in the annual timetable mode. The author marked the calculated break-even point in the number of route-days as the unknown  $x$ . For the system to work, the price of railway capacity allocation for RJ, PJ or ZJ for  $x-1$  and fewer route-days should be higher than the price of railway capacity allocation for N3 for  $x-1$  and fewer route-days. For limit number of route-days, the following inequalities (2), (3), (4), and (5) apply.

$$(RJ, PJ, ZJ) \leq C(N3) \quad (2)$$

$$K1 + K2 \cdot DtrRJ + K3 \cdot PdJRJxN3 \leq K1 + K2 \cdot DtrRJ + K3 \cdot PdJRJxN3 \quad (3)$$

$$K1 + K2 \cdot DtrPJ + K3 \cdot PdJPJxN3 \leq K1 + K2 \cdot DtrPJ + K3 \cdot PdJPJxN3 \quad (4)$$

$$K1 + K2 \cdot DtrZJ + K3 \cdot PdJZJxN3 \leq K1 + K2 \cdot DtrZJ + K3 \cdot PdJZJxN3 \quad (5)$$

Where:

(RJ) is the price of railway capacity allocation for RJ [CZK],

(PJ) is the price of railway capacity allocation for PJ [CZK],

(ZJ) is the price of railway capacity allocation for ZJ [CZK],

(N3) is the price of railway capacity allocation for N3 [CZK],

$K1$  is the price of processing and determining of the timetable and railway capacity allocation [CZK],

$K2$  is the price of train route creation [CZK per km],

$K3$  is the price of route allocation per day [CZK per day],

$DtrRJ$  is the length of the average RJ route; the distance between point of origin and point of destination on railway network, where the Railway Infrastructure Administration functions as infrastructure manager, or capacity allocator [km],

$DtrPJ$  is the length of the average PJ route; the distance between point of origin and point of destination on railway network, where the Railway Infrastructure Administration functions as infrastructure manager, or capacity allocator [km],

$DtrZJ$  is the length of the average PJ route; the distance between point of origin and point of destination on railway network, where the Railway Infrastructure Administration functions as infrastructure manager, or capacity allocator [km],

$PdJRJxN3$  limit number of route-days for RJ compared with N3 the respective route is allocated for [day],

$PdJPJxN3$  limit number of route-days for PJ compared with N3 the respective route is allocated for [day],

$PdJZJxN3$  limit number of route-days for ZJ compared with N3 the respective route is allocated for [day],

The calculation was made according to formulas (3), (4) and (5), where the number of route-days  $Pdj$  was used as the unknown  $x$ .

After substitution, the inequation for RJ is as follows:

$$K1RJ + K2RJ \cdot DtrRJ + K3RJ \cdot PdJRJxN3 \leq K1N3 + K2N3 \cdot DtrRJxN3 + K3N3 \cdot PdJRJxN3 \quad (6)$$

$$1700 + 8 \cdot 53.5 + 10 \cdot x \leq 100 + 0 \cdot 53.5 + 70 \cdot x$$

$$33.8 \leq x$$

The limit value  $x$  for the number of route-days for RJ was rounded to 34. The same substitution was performed for products PJ and ZJ. The results are interpreted in Table 12.

After substitution, the inequation for PJ is as follows:

$$K1PJ + K2PJ \cdot DtrPJ + K3PJ \cdot PdJPJxN3 \leq K1N3 + K2N3 \cdot DtrPJxN3 + K3N3 \cdot PdJPJxN3 \quad (7)$$

$$1700 + 10 \cdot 47.8 + 20 \cdot x \leq 100 + 0 \cdot 47.8 + 70 \cdot x$$

$$41.6 \leq x$$

The limit value  $x$  for the number of route-days for PJ was rounded to 42.

After substitution, the inequation for ZJ is as follows:

$$K1ZJ + K2ZJ \cdot DtrZJ + K3ZJ \cdot PdJZJ \leq K1N3 + K2N3 \cdot DtrZJxN3 + K3N3 \cdot PdJZJxN3 \quad (8)$$

$$1700 + 10 \cdot 69.5 + 20 \cdot x \leq 100 + 0 \cdot 69.5 + 70 \cdot x$$

$$45.9 \leq x$$

The limit value  $x$  for the number of route-days for ZJ was rounded to 46. The calculated limit values are summarised in Table 6.

Table 6. Calculated limit values for allocated route-days and comparison of prices for selected products

Product	RJ	PJ	ZJ
<b>Number of route-days x-1</b>	<b>33</b>	<b>41</b>	<b>45</b>
Price of product RJ, PJ, ZJ [CZK]	2,458	2,998	3,295
Price of product N3 [CZK]	2,410	2,970	3,250
<b>Limit number of route-days x</b>	<b>34</b>	<b>42</b>	<b>46</b>
Price of product RJ, PJ, ZJ [CZK]	2,468	3,018	3,315
Price of product N3 [CZK]	2,480	3,040	3,320

Source: Authors

The Table shows that with 34 and more allocated route-days for RJ, the price of allocated railway capacity is lower than the price of railway capacity allocation for N3 with the current coefficients K1, K2 and K3. With 42 and more allocated route-days for PJ, the price of allocated railway capacity is lower than the price of railway capacity allocation for N3.

With 46 and more allocated route-days for ZJ, the price of allocated railway capacity (for the average route length of RJ, PJ and ZJ) is lower than the price of railway capacity allocation for N3.

The aim of the proposed change to the price of railway capacity allocation was for the price to have a regulatory function and at the same time, to cover the direct costs incurred by the Railway Infrastructure Administration in connection with railway capacity allocation, with the revenue from the railway capacity allocation not exceeding these direct costs. Economic assessment was conducted on the timetable 2016 data. The direct costs of railway capacity allocation stated in the annual report of the Railway Infrastructure Administration (25) were established by the Railway Infrastructure Administration economic department to be about CZK 106,780,000.

### 3. Creating a model for calculation

The authors start from the consideration that the total amount collected for railway capacity allocation (revenue from railway capacity allocation) must be lower or equal to the direct costs of railway capacity allocation. The following relation thus applies:

$$\sum_{c=1}^{c=10} v_c \leq \sum_{c=1}^{c=10} n_c \quad (9)$$

Where:

$v_c$  is the total revenue from railway capacity allocation [CZK],

$n_c$  are the total direct costs of rail capacity allocation [CZK].

The individual  $v_c$  products are marked as follows:  $v_1$  is the price of capacity allocation for individual requests for RJ,  $v_2$  is the price of capacity allocation for individual requests for PJ,  $v_3$  is the price of capacity allocation for individual requests for ZJ,  $v_4$  is the price of capacity allocation for individual requests for N3,  $v_5$  is the price of capacity allocation for individual requests for P3,  $v_6$  is the price of capacity allocation for individual requests for TB,  $v_7$  is the price of capacity allocation for individual requests for ZK,  $v_8$  is the price of capacity allocation for individual requests for UI,  $v_9$  is the price of capacity allocation for individual requests for OM, and  $v_{10}$  is the price of capacity allocation for individual requests for JD. For these  $v_c$  the following relations apply:



$$v_1 = \sum_{n=1}^{n=c_1} (K_{1RJ} + K_{2RJ} \cdot D_{trRJn} + K_{3RJ} \cdot P_{djRJn}) \quad [\text{CZK}] \quad (10)$$

$$v_2 = \sum_{n=1}^{n=c_2} (K_{1PJ} + K_{2PJ} \cdot D_{trPJn} + K_{3PJ} \cdot P_{djPJn}) \quad [\text{CZK}] \quad (11)$$

$$v_3 = \sum_{n=1}^{n=c_3} (K_{1ZJ} + K_{2ZJ} \cdot D_{trZJn} + K_{3ZJ} \cdot P_{djZJn}) \quad [\text{CZK}] \quad (12)$$

$$v_4 = \sum_{n=1}^{n=c_4} (K_{1N3} + K_{2N3} \cdot D_{trN3n} + K_{3N3} \cdot P_{djN3n}) \quad [\text{CZK}] \quad (13)$$

$$v_5 = \sum_{n=1}^{n=c_5} (K_{1P3} + K_{2P3} \cdot D_{trP3n} + K_{3P3} \cdot P_{djP3n}) \quad [\text{CZK}] \quad (14)$$

$$v_6 = \sum_{n=1}^{n=c_6} (K_{1TB} + K_{2TB} \cdot D_{trTBn} + K_{3TB} \cdot P_{djTBn}) \quad [\text{CZK}] \quad (15)$$

$$v_7 = \sum_{n=1}^{n=c_7} (K_{1ZK} + K_{2ZK} \cdot D_{trZKn} + K_{3ZK} \cdot P_{djZKn}) \quad [\text{CZK}] \quad (16)$$

$$v_8 = \sum_{n=1}^{n=c_8} (K_{1UI} + K_{2UI} \cdot D_{trUIn} + K_{3UI} \cdot P_{djUIn}) \quad [\text{CZK}] \quad (17)$$

$$v_9 = \sum_{n=1}^{n=c_9} (K_{1OM} + K_{2OM} \cdot D_{trOMn} + K_{3OM} \cdot P_{djOMn}) \quad [\text{CZK}] \quad (18)$$

$$v_{10} = \sum_{n=1}^{n=c_{10}} (K_{1JD} + K_{2JD} \cdot D_{trJDn} + K_{3JD} \cdot P_{djJDn}) \quad [\text{CZK}] \quad (19)$$

Under the following conditions:

$$(K_{1RJ} + K_{2RJ} \cdot D_{trRJm} + K_{3RJ} \cdot P_{djRJm}) < (K_{1N3} + K_{2N3} \cdot D_{trN3m} + K_{3N3} \cdot P_{djN3m}) \quad (20)$$

$$(K_{1RJ} + K_{2RJ} \cdot D_{trRJm} + K_{3RJ} \cdot P_{djRJm}) < (K_{1PJ} + K_{2PJ} \cdot D_{trPJm} + K_{3PJ} \cdot P_{djPJm}) \quad (21)$$

$$(K_{1RJ} + K_{2RJ} \cdot D_{trRJm} + K_{3RJ} \cdot P_{djRJm}) < (K_{1ZJ} + K_{2ZJ} \cdot D_{trZJm} + K_{3ZJ} \cdot P_{djZJm}) \quad (22)$$

$$(K_{1N3} + K_{2N3} \cdot D_{trN3m} + K_{3N3} \cdot P_{djN3m}) < (K_{1P3} + K_{2P3} \cdot D_{trP3m} + K_{3P3} \cdot P_{djP3m}) \quad (23)$$

$$(K_{1PJ} + K_{2PJ} \cdot D_{trPJ} + K_{3PJ} \cdot P_{djPJ}) < (K_{1N3} + K_{2N3} \cdot D_{trN3} + K_{3N3} \cdot P_{djN3}) \quad (24)$$

$$(K_{1ZJ} + K_{2ZJ} \cdot D_{trZJ} + K_{3ZJ} \cdot P_{djZJ}) < (K_{1N3} + K_{2N3} \cdot D_{trN3} + K_{3N3} \cdot P_{djN3}) \quad (25)$$

$$K_{1RJ} + K_{2RJ} \cdot D_{trRJ} + K_{3RJ} \cdot (P_{dj} - 1)_{RJ} > K_{1N3} + K_{2N3} \cdot D_{trN3} + K_{3N3} \cdot (P_{dj} - 1)_{N3} \quad (26)$$

$$K_{1PJ} + K_{2PJ} \cdot D_{trPJ} + K_{3PJ} \cdot (P_{dj} - 1)_{PJ} > K_{1N3} + K_{2N3} \cdot D_{trN3} + K_{3N3} \cdot (P_{dj} - 1)_{N3} \quad (27)$$

Where:

$n$  is the number of kilometres, route-days of the  $n$ th request for railway capacity for product  $cn$ ,  $n = 1, 2, 3, \dots, cn$ ,

$m$  is the number of limit kilometres, route-days for product  $cn$ ,  $m = 1, 2, 3, \dots, m$ ,

$n = cn$  is the total number of requests for railway capacity for product  $cn$ ,

$vc1, vc2, vc3, \dots, vc10$  is the revenue from railway capacity allocation for product  $c1, c2, c3, \dots, c10$  [CZK],

$c1, c2, c3, \dots, c10$  is the total number of requests for railway capacity for product (RJ, PJ, ZJ, N3, P3,

TB, ZK, UI, OM and JD) [CZK],

$K1$  is the price of processing and determining of the timetable and railway capacity allocation [CZK per route],

$K2$  is the price of train route creation [CZK per km],

$K3$  is the price of train route allocation per day [CZK per day],

$DtrRJ, DtrPJ, DtrZJ, DtrN3, DtrP3, DtrTB, DtrZK, DtrUI, DtrOM, DtrJD$  is the route length for products (RJ, PJ, ZJ, N3, P3, TB, ZK, UI, OM, JD), the distance between point of origin and point of destination on railway network, where the Railway Infrastructure Administration functions as infrastructure manager, or capacity allocator [km],

$PdjRJ, PdjPJ, PdjZJ, PdjN3, PdjP3, PdjTB, PdjZK, PdjUI, PdjOM, PdjJD$  is the number of route-days for RJ the respective route is allocated for [day],

The authors didn't include UI, OM a JD in the calculations as they do not factor in the price of railway capacity allocation as in accordance with applicable legal provisions, their price hasn't been set.

The authors simplified inequations (20), (21), (22) and (23) in the way described below, creating several invariables. Since coefficient  $K1$  is the price of request processing, all requests processed in IS KANGO16 (products RJ, PJ and ZJ) have the same  $K1$ , and requests processed in IS KADR (products N3 and P3) have the same coefficient  $K1$ . The ratio between  $K1$  value for requests processed in IS KANGO and requests processed in IS KADR is based on the current ratio and was established as 0.06. For coefficient  $K1$  for individual products, the author established the following relations:

$$K1RJ = K1RJ$$

$$K1PJ = K1RJ$$

$$K1ZJ = K1RJ$$

The authors first modelled Option 0 reflecting the current situation and the current allocation charging scheme using the current coefficients K1, K2 and K3.

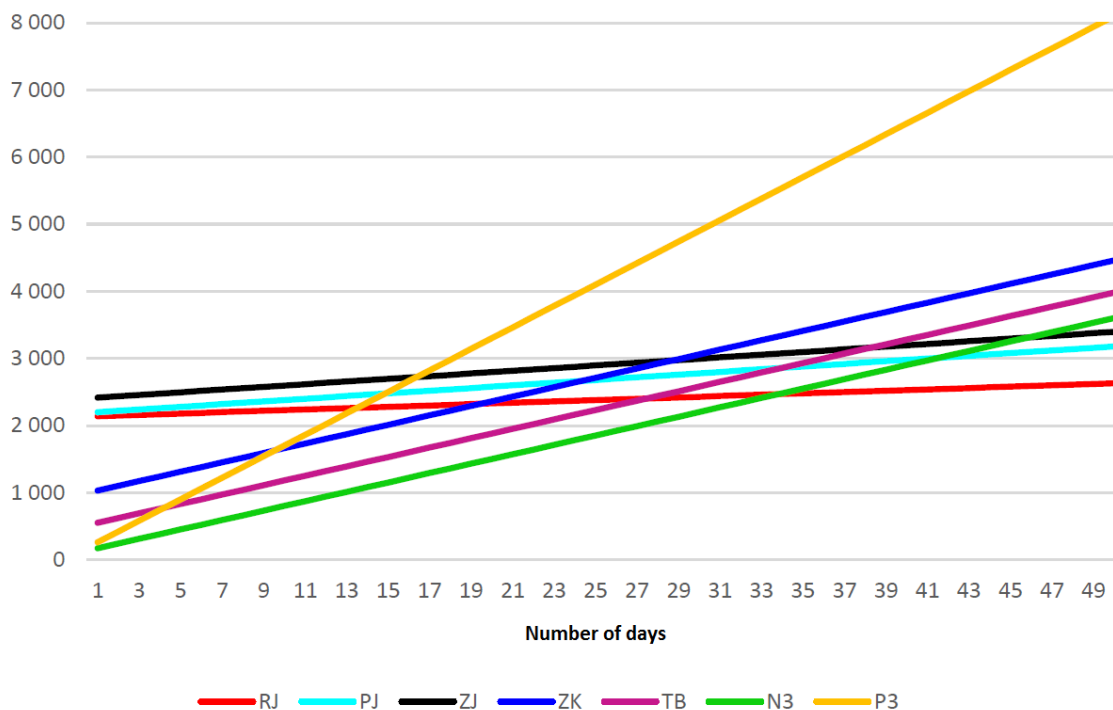
Table 7. Calculation for all requests based on coefficients (for total values)

Product	K1	Number of data timetables	K2	Total number of kilometres	K3	Number of route-days	Price of product [CZK]	Ø price of 1 request [CZK]
<b>RJ</b>	1,700	13,686	8	731,593	10	2,899,051	58,109,454	4,246
<b>PJ</b>	1,700	788	10	37,661	20	132,265	4,361,513	5,534
<b>ZJ</b>	1,700	485	10	33,727	20	32,170	1,805,166	3,721
<b>ZK</b>	960	285	0	11,492	70	367	299,290	1,051
<b>TB</b>	480	196	0	9,742	70	196	107,800	550
<b>N3</b>	100	13,534	0	1,357,650	70	26,400	3,201,400	240
<b>P3</b>	100	159,968	0	11,491,204	160	160,943	41,747,680	260
<b>Total price [CZK]</b>							<b>109,632,303</b>	<b>15,602</b>

Source: Authors

The total price in Table 7 is the current revenue from railway capacity allocation. The current direct costs of railway capacity allocation were established by the Railway Infrastructure Administration economic department to be about CZK 106,780,000. This amount shouldn't be exceeded. The difference between revenue and costs is approximately 2.67% (CZK 2,852,303). It is approximately this amount the revenue from railway capacity allocation needs to be reduced by while complying with the conditions of formulas (20), (21) ~ (22), (23), (24) ~ (25), (26) and (27). The break-even point of price between products is shown in Figure 1.

CZK



Source: Authors

Fig. 1. The break-even point of price between products

Table 8 Comparison of revenue from railway capacity allocation with total direct costs of railway capacity allocation

Revenue from railway capacity allocation [CZK]		Costs of railway capacity allocation [CZK]	Difference between revenue and costs [%]
109,632,303	>	106,780,000	2.67

Source: Authors

## 4. Summary

Current model for calculation of the price of railway capacity allocation using coefficients K1, K2, and K3 in accordance with Table 8. In 2016, the revenue from railway capacity allocation was 2.67% higher than the total direct costs of railway capacity allocation.

In this paper, the authors defined the requirements on target groups of requests so that they can be attributed to individual products either in the mode of allocating railway capacity within the annual timetable, or in the ad hoc mode. This definition is vital for proper regulation of the demand of railway undertakings for individual products. The aim of the proposed model is for a part of the requests to move from the ad hoc mode to the annual timetable mode.

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